

P P SAVANI UNIVERSITY

Third Semester of B. Tech. Examination

December 2022

SESH2011 Differential Equations

23.11.2022, Wednesday

Time: 10:00 a.m. To 12:30 p.m.

Maximum Marks: 60

Instructions:

1. The question paper comprises of two sections.
2. Section I and II must be attempted in separate answer sheets.
3. Make suitable assumptions and draw neat figures wherever required.
4. Use of scientific calculator is allowed.

SECTION - I

- Q - 1 Choose correct answer for any two:** [05] CO BTL
- (i) Degree of the differential equation $y = z \frac{dy}{dx} + \frac{x}{\frac{dy}{dx}}$ is _____. [1] 1/2
 a. 1 b. 2 c. 3 d. 4
- (ii) The necessary condition for the differential equation to be an exact differential equation is _____. [2] 1
 a. $\frac{\partial N}{\partial y} \neq \frac{\partial M}{\partial x}$ b. $\frac{\partial N}{\partial x} = \frac{\partial M}{\partial x}$ c. $\frac{\partial M}{\partial x} = \frac{\partial N}{\partial y}$ d. $\frac{\partial M}{\partial y} = \frac{\partial N}{\partial x}$
- (iii) The root of the PDE $(2D^2 + 5DD' + 2D'^2)z = 0$ is _____. [2] 2
 a. $(2, -\frac{1}{2})$ b. $(-2, \frac{1}{2})$ c. $(2, \frac{1}{2})$ d. $(-2, -\frac{1}{2})$
- Q - 2 (a)** Solve $x^2(y - z)p + y^2(z - x)q = z^2(x - y)$. [05] 2 5
Q - 2 (b) Solve $(x^2 + y^2 + 1)dx - 2xydy = 0$. [05] 1 4/5
- OR**
- Q - 2 (a)** Solve $\frac{y^2z}{x}p + xzq = y^2$. [05] 2 5
Q - 2 (b) Solve $2xyy' = y^2 - x^2$. [05] 1 4/5
Q - 3 Solve $\frac{\partial u}{\partial x} + \frac{\partial u}{\partial y} = 2(x + y)u$. [05] 2 5
- OR**
- Q - 3** Solve $z = px + qy - 2\sqrt{pq}$. [05] 2 3/5
Q - 4 Attempt any one: [10]
- (i) Find the orthogonal trajectory of $r = a(1 - \cos \theta)$. [1] 4
 (ii) Solve $\frac{d^2y}{dx^2} + \frac{dy}{dx} - 12y = e^{6x}$. [1] 5

SECTION - II

- Q - 1 Choose correct answer for any two:** [05]
- (i) Which of the following is not periodic functions? [5] 1/2
 a. x b. e^x c. $\ln x$ d. All
- (ii) Which of the following is odd function. [5] 1/2
 a. $\cos x$ b. $\tan x$ c. x^2 d. None
- (iii) $L\{\cosh at\} =$ _____. [4] 1
 a. $\frac{s}{s^2+a^2}$ b. $\frac{a}{s^2-a^2}$ c. $\frac{a}{s^2+a^2}$ d. $\frac{s}{s^2-a^2}$
- Q - 2 (a)** Find the Fourier series of $f(x) = \begin{cases} \pi x & 0 \leq x \leq 1 \\ \pi(2-x) & 1 \leq x \leq 2 \end{cases}$. [05] 5 4
Q - 2 (b) Find the Laplace transform of $\frac{1-e^{-t}}{t}$. [05] 4 5
- OR**
- Q - 2 (a)** Find the Fourier series of $f(x) = e^{-x}$ in the interval $0 < x < 2\pi$. [05] 5 5

- Q - 2 (b) Find the Laplace transform of $\int_0^t e^{-t} dt$. [05] 4 5
 Q - 3 Find the Fourier cosine and Fourier sine transforms of [05] 4 4/5

$$f(x) = \begin{cases} k & 0 < x < a \\ 0 & x > a \end{cases}$$

OR

- Q - 3 Find the half-range cosine series $f(x) = \sin x$ in the interval $(0, \pi)$. [05] 4 5
 Q - 4 **Attempt any one:** [10]
 (i) Using Fourier integral representation, show that 4 4/5

$$\int_0^\infty \frac{\cos \omega x + \omega \sin \omega x}{1 + \omega^2} d\omega = \begin{cases} 0 & x < 0 \\ \frac{\pi}{2} & x = 0 \\ \pi e^{-x} & x > 0 \end{cases}$$

- (ii) Find the Laplace transform of 4 5
 $f(t) = \begin{cases} 4; & 0 \leq t < 1 \\ 3; & t \geq 1 \end{cases}$

CO : Course Outcome Number

BTL : Blooms Taxonomy Level

Level of Bloom's Revised Taxonomy in Assessment

1: Remember	2: Understand	3: Apply
4: Analyze	5: Evaluate	6: Create